



201															
eqī	а	g	С	t	t	а	С	С	t	g	t	t	а	С	t
eq 2	С	g	t	а	а	а	t	t	t	С	С	С	g	а	t
eq 3	С	g	С	а	а	g	t	t	t	С	С	С	g	а	t
eq 4	С	а	С	t	t	а	t	t	а	g	t	С	а	а	С





Maximum Parsimony I

A rule in science and philosophy stating that entities should not be multiplied needlessly.

This rule is interpreted to mean that the simplest of two or more competing theories is preferable and that an explanation for unknown phenomena should first be attempted in terms of what is already known.

Also called law of parsimony. (Ockham's razor, ca 1285-1350)









				I	Dist	anc	e b	ase	ed m	netl	node	s I:					
	seq 1	а	g	с	t	t	а	с	с	t	g	t	t	а	с	t	
	seq 2	с	g	t	а	а	а	t	t	t	с	с	с	g	а	t	
	seq 3	с	g	с	а	а	g	t	t	t	с	с	с	g	а	t	
	seq 4	с	а	с	t	t	а	t	t	а	g	t	с	а	а	С	
								ļ	$(a_i$,),	<i>j</i> -1.					_	
					S	eq	1	Se	eq 2	2	Sec	q 3	S	Seq	4		
			Seq	1	0			11			11		8				
			Seq	2	1	1		0			2		1	0			
			Seq	3	1	1		2			0		9				
			Seq 4			8			10			9			0		
1		_														-	













Distance based methods: Neighbor joining III

6. compute distance W to the remaining m-2 leaves:

$$D(W,k) = \frac{1}{2} (D(A,k) + D(B,k) - D(A,B))$$







Find a tree τ that minimizes

Г

$$S(\tau) = \sum_{i,k} \left(\rho(i,k) - D(i,k) \right)^2$$

where $\rho(i,k)$ is the length of the unique path connecting leaves *i* and *k* in the tree.



Distance based metho	ods: Least Square III
$d_{12} = b_1 + b_2$ $d_{13} = b_1 + b_3 + b_6$	d = Ab
$d_{14} = b_1 + b_4 + b_6 + b_7$ $d_{15} = b_1 + b_5 + b_6 + b_7$ $d_{23} = b_2 + b_3 + b_6$ $d_{24} = b_2 + b_4 + b_6 + b_7$ $d_{25} = b_2 + b_5 + b_6 + b_7$ $d_{34} = b_3 + b_4 + b_7$ $d_{35} = b_3 + b_5 + b_7$ $d_{44} = b_4 + b_5$	$\boldsymbol{A} = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 \end{bmatrix},$

Distance based methods: Least Square IV

Least square estimates of the branch lengths

$$\hat{\boldsymbol{b}} = (\boldsymbol{A}^{t}\boldsymbol{A})^{-1}\boldsymbol{A}^{t}\boldsymbol{d}$$